



Interaction Effects

in MPlus



Intro

Today's goal:

Teach how to test condition*factor and factor*factor interaction effects

Outline:

- Overview of interaction effects and approaches
- The random slopes approach
- The multiple groups approach



Overview

of interaction effects



Interaction effects

What is the combined effect of x_1 and x_2 on y ?

Possibilities:

Additive effect

Super-additive effect

Sub-additive effect

Cross-over

	$x_1 = \text{low}$	$x_1 = \text{high}$
$x_2 = \text{low}$	0	5
$x_2 = \text{high}$	5	10



Interaction effects

What is the combined effect of x_1 and x_2 on y ?

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Sub-additive effect

Cross-over

	$x_1 = \text{low}$	$x_1 = \text{high}$
$x_2 = \text{low}$	0	5
$x_2 = \text{high}$	5	15



Interaction effects

What is the combined effect of x_1 and x_2 on y ?

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Sub-additive effect

Cross-over

	$x_1 = \text{low}$	$x_1 = \text{high}$
$x_2 = \text{low}$	0	5
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Interaction effects

What is the combined effect of x_1 and x_2 on y ?

Possibilities:

Additive effect

Super-additive effect

Sub-additive effect

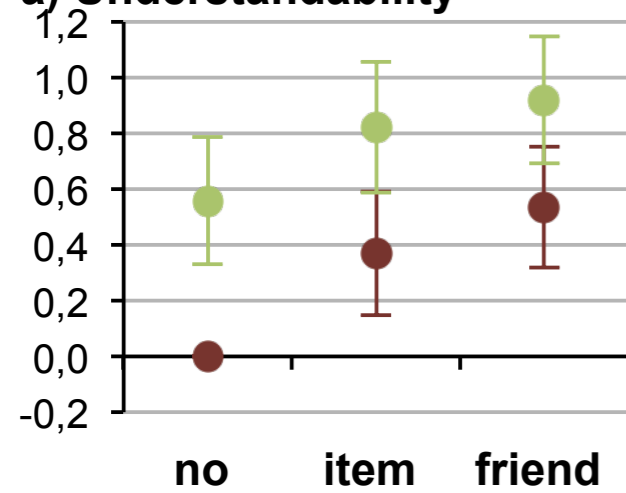
Cross-over

	$x_1 = \text{low}$	$x_1 = \text{high}$
$x_2 = \text{low}$	0	5
$x_2 = \text{high}$	5	0

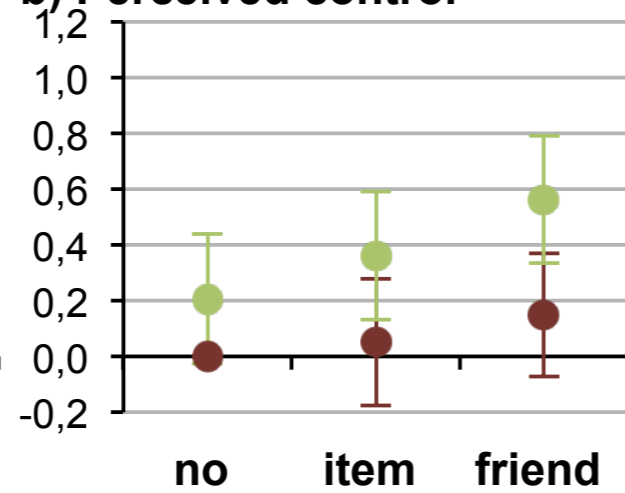


Examples

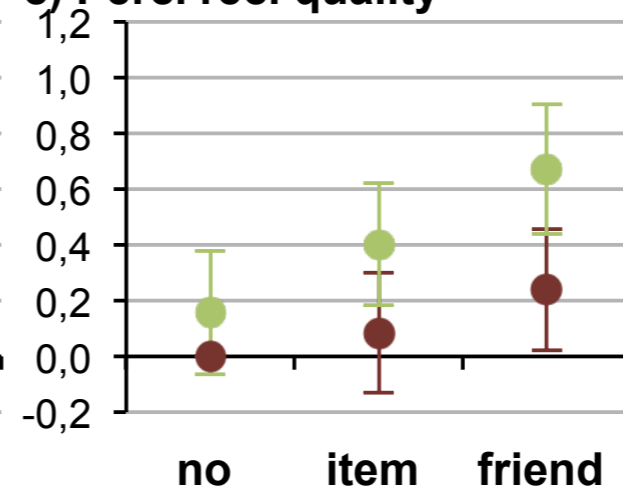
a) Understandability



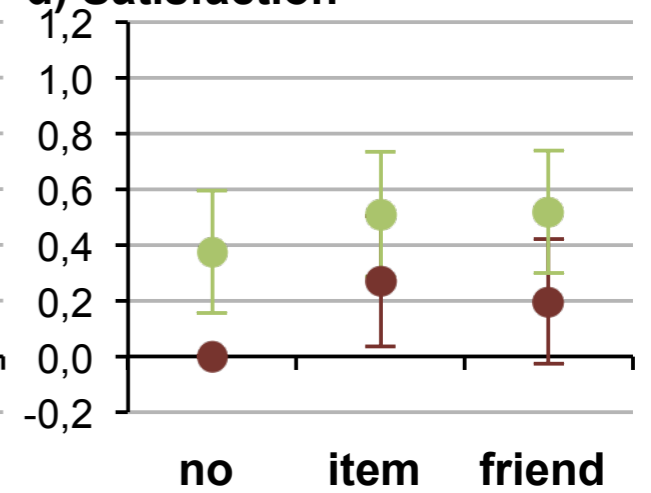
b) Perceived control



c) Perc. rec. quality

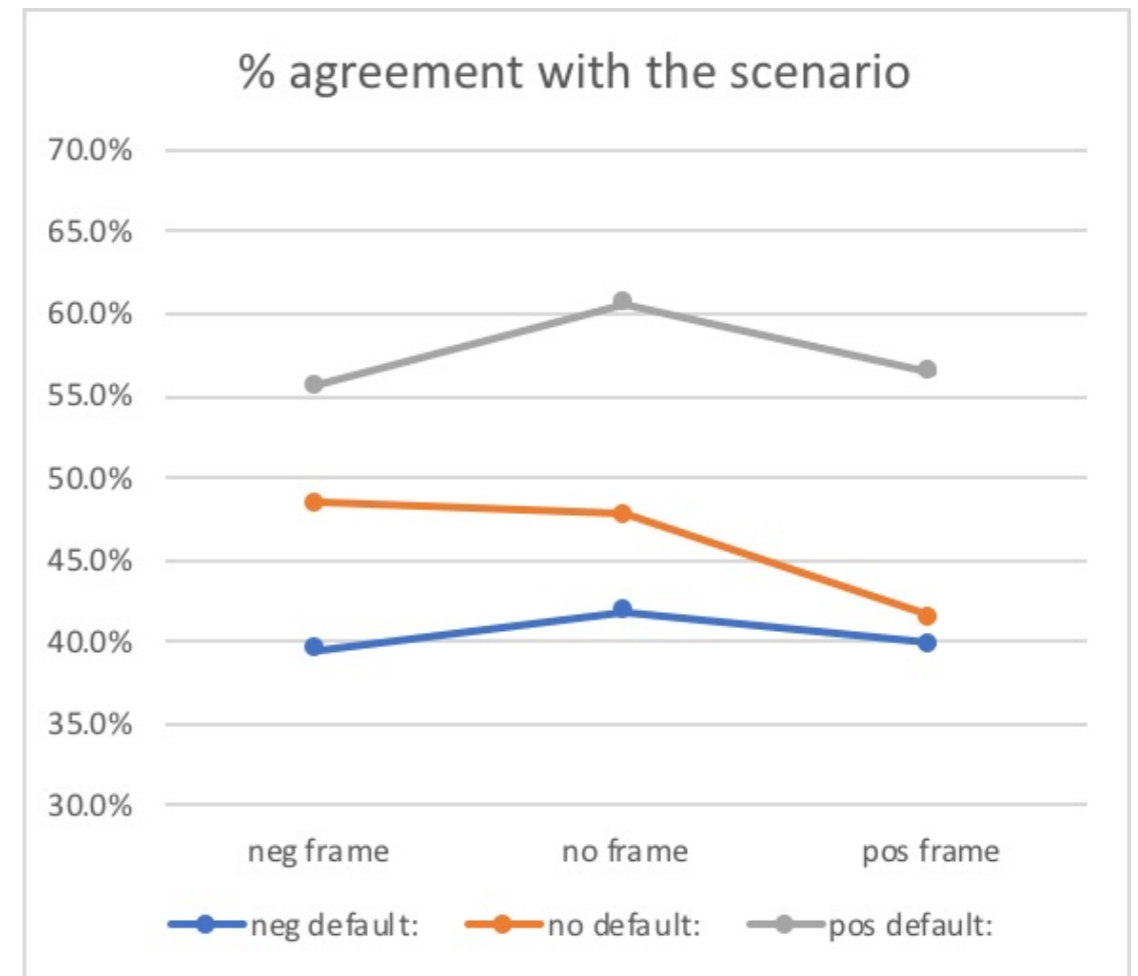
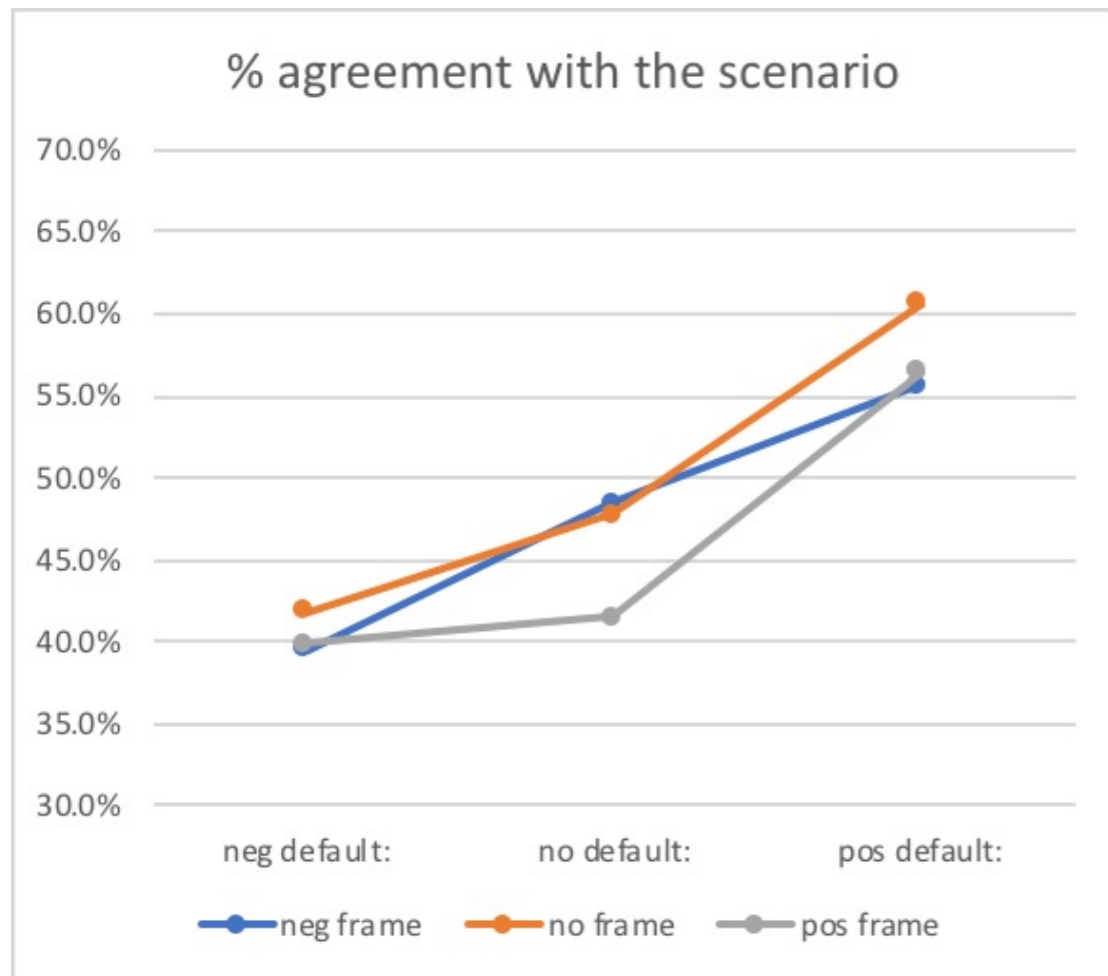


d) Satisfaction





Fresh example





Outputs

Additive effect

x1	5.000	
x2	5.000	
x1*x2	0.000	(n.s.)

Super-additive effect

x1	5.000	
x2	5.000	
x1*x2	5.000	(sig)

Sub-additive effect

x1	5.000	
x2	5.000	
x1*x2	-5.000	(sig)

Cross-over effect

x1	5.000	
x2	5.000	
x1*x2	-10.000	(sig)



Model specification

This is easy in regressions

Just multiply the dependent variables!

$$y \sim x1 * x2$$

More difficult in SEM

Depends on type of variables:

manipulation * manipulation

manipulation * factor

factor * factor



Model specification

manipulation * manipulation is easy:

Just create the dummies!

See SEM slides and homework for an example

manipulation * factor:

Multiple groups model or predicted random slopes model

factor * factor:

Predicted random slopes model



Two approaches

“Predicted random slopes model”

Pro: Works for all types of variables

Con: Cannot use categorical indicators

Con: Can take a long time to estimate

“Multiple groups model”

Pro: Easier to estimate

Pro: Can sometimes use categorical indicators*

Con: Does not work for factor * factor interactions



Random slopes approach

for factor*condition and factor*factor interaction effects



Random slopes

Under ANALYSIS:

Specify random slopes (type = random)

Specify integration (algorithm = integration)

Under MODEL:

Specify the moderated effect as random: $s \mid y$ on x ;

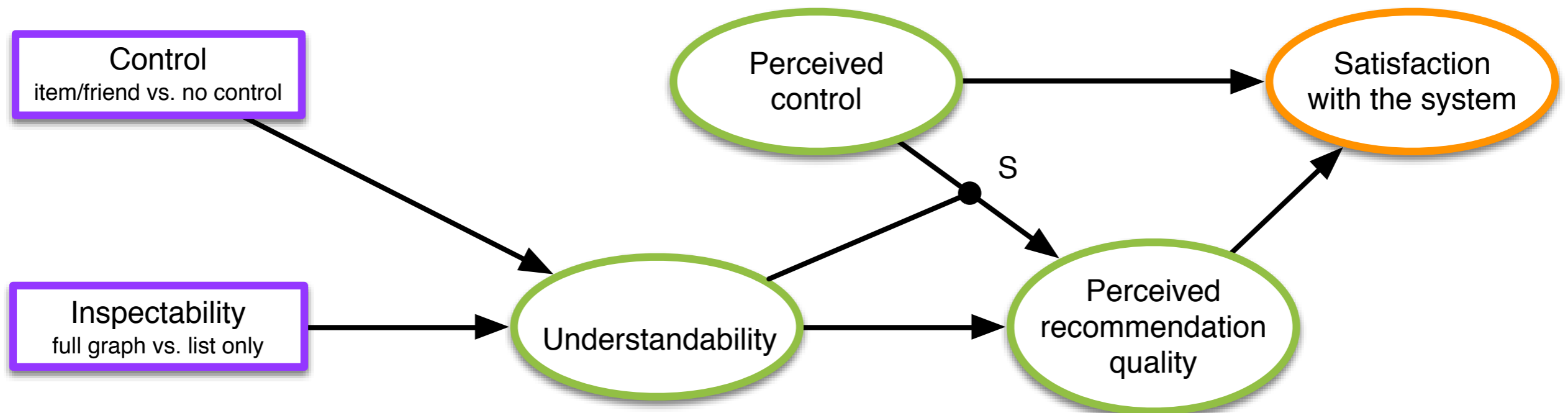
Regress the slope on the moderator: s on m ;

Add main effect of moderator: y on m ;



Factor * factor

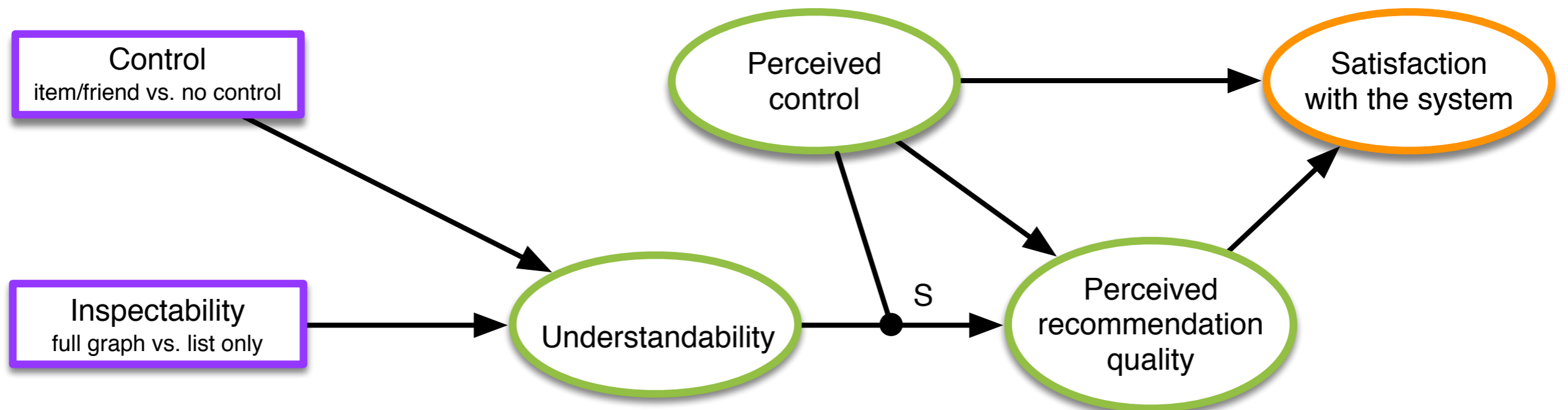
Example: is the effect of perceived control on perceived recommendation quality dependent on understandability?





Factor * factor

Equivalent: is the effect of understandability on perceived recommendation quality dependent on perceived control?





Factor * factor

slopes1.inp

Specify the model as UVI

Under model, add:

```
s | quality ON control;
```

```
s ON underst;
```

```
quality ON underst;
```

In regression terms, this would simply be:

```
quality ~ control*underst
```



Factor * factor

SATISF	ON				
QUALITY		0.401	0.097	4.114	0.000
CONTROL		-0.924	0.155	-5.979	0.000
S	ON				
UNDERST		0.047	0.081	0.579	0.563
QUALITY	ON				
UNDERST		0.061	0.078	0.776	0.438
UNDERST	ON				
CITEM		0.348	0.160	2.180	0.029
CFRIEND		0.474	0.164	2.888	0.004
CGRAPH		0.535	0.135	3.969	0.000
Intercepts:					
S		-0.771	0.111	-6.962	0.000



Factor * factor

slopes1a.inp

Under model, add:

```
s | quality ON underst;
```

```
s ON control;
```

```
quality ON control;
```

This model is equivalent



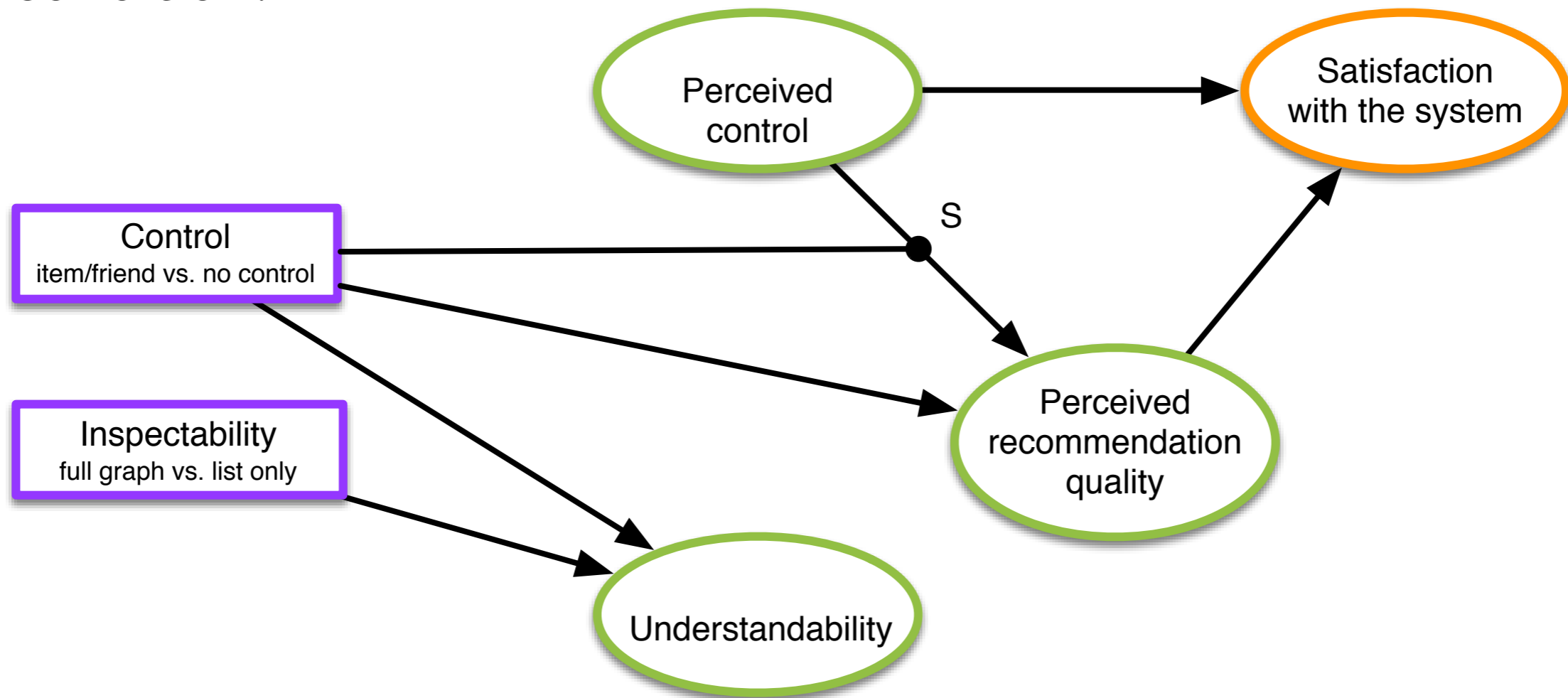
Factor * factor

SATISF	ON				
QUALITY		0.280	0.106	2.655	0.008
CONTROL		-0.916	0.158	-5.814	0.000
S	ON				
CONTROL		0.094	0.119	0.790	0.429
QUALITY	ON				
CONTROL		-1.094	0.347	-3.153	0.002
UNDERST	ON				
CITEM		0.257	0.153	1.686	0.092
CFRIEND		0.367	0.169	2.172	0.030
CGRAPH		0.452	0.139	3.247	0.001
Intercepts:					
S		0.056	0.110	0.506	0.613



Factor * condition

Example: is the effect of perceived control on perceived recommendation quality dependent on the control condition?





Factor * condition

slopes2.inp

Under model, add:

s | quality ON control;

s ON citem cfriend;

quality ON citem cfriend;



Factor * condition

SATISF	ON				
QUALITY		0.373	0.092	4.041	0.000
CONTROL		-0.909	0.159	-5.733	0.000
S	ON				
CITEM		-0.108	0.171	-0.634	0.526
CFRIEND		0.565	0.165	3.418	0.001
QUALITY	ON				
CITEM		0.052	0.159	0.329	0.742
CFRIEND		0.288	0.172	1.674	0.094
UNDERST	ON				
CITEM		0.327	0.160	2.044	0.041
CFRIEND		0.486	0.161	3.019	0.003
CGRAPH		0.509	0.134	3.815	0.000
Intercepts:					
S		-0.955	0.145	-6.583	0.000



Multiple group approach

for factor*condition interaction effects



Multiple groups

Under VARIABLE:

Specify the moderating manipulation as a “grouping” variable: `grouping = cctrl(0=none 1=item 2=friend)`

Add a MODEL section for all groups except the baseline

Model item:

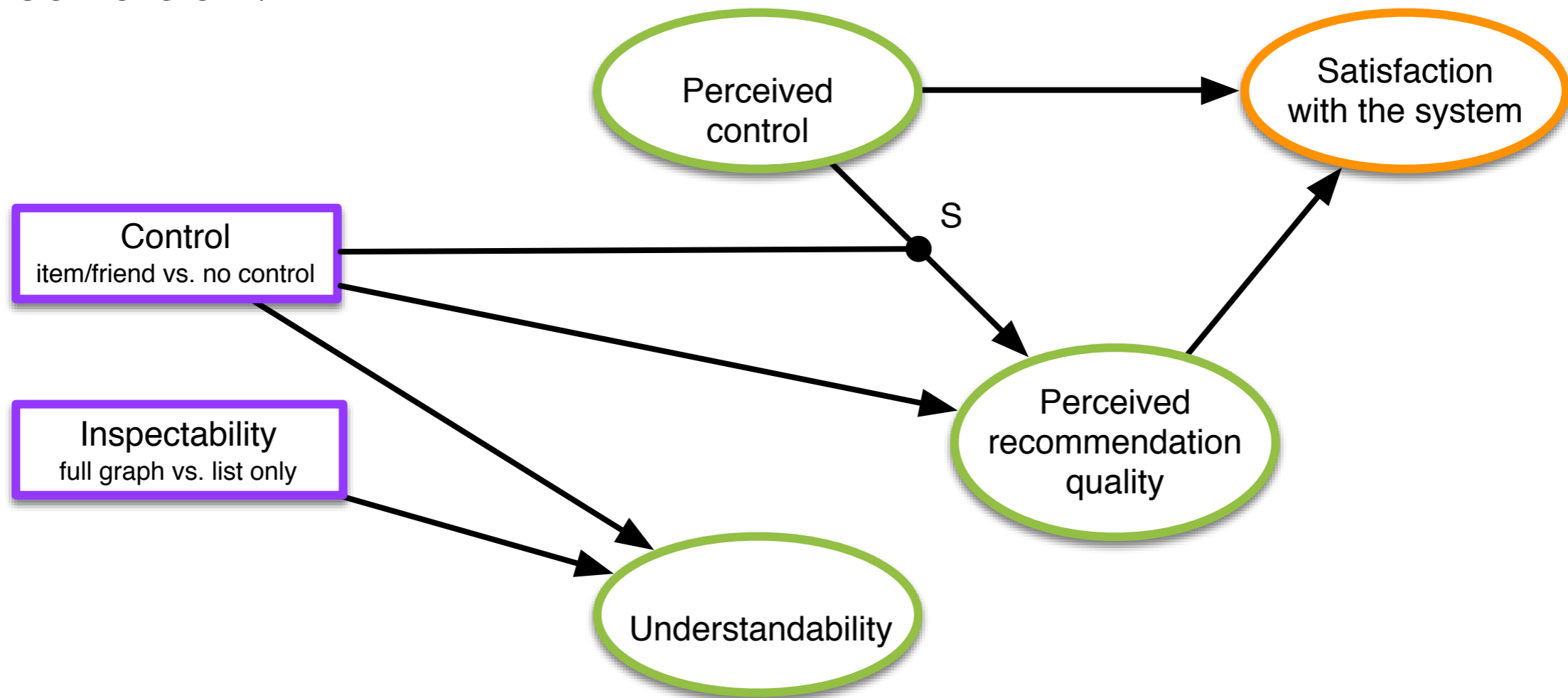
Model friend:

Add corresponding labels to each MODEL to restrict the moderation



Factor * condition

Example: is the effect of perceived control on perceived recommendation quality dependent on the control condition?





Factor * condition

multi.inp

MODEL:

```
satisf BY s1* s2-s7;  
quality BY q1* q2-q6;  
control BY c1* c2-c4;  
underst BY u2* u4-u5;  
satisf-underst@1;
```

```
satisf ON quality control (1-2);  
quality ON control (p1);  
control ON underst (4);  
underst ON cgraph (5);
```

MODEL item:

```
satisf ON quality control (1-2);  
quality ON control (p2);  
control ON underst (4);  
underst ON cgraph (5);
```

```
[satisf] (p4);  
[control] (p5);
```

MODEL friend:

```
satisf ON quality control (1-2);  
quality ON control (p3);  
control ON underst (4);  
underst ON cgraph (5);
```

```
[satisf] (p4);  
[control] (p5);
```

MODEL CONSTRAINT:

```
p4=0;  
p5=0;
```

MODEL TEST:

```
p1=p3;
```



Factor * condition

*** ERROR

Based on Group 2: Group 0 contains
inconsistent categorical value for Q6: 2

Problem:

There are three groups (0=none, 1=item and 2=friend)

Q6 has 5 possible values (-2, -1, 0, 1, 2)

Mplus tries to estimate the same thresholds in each group

But in group 0, nobody has the value 2 on Q6!



Factor * condition

Possible solutions:

Collapse values 1 and 2

Under DEFINE: `if(Q6 EQ 2) then Q6 = 1;`

Repeat for other variables, see multi-alt.inp

Simply run the model without categorical variables

Remove categorical are s1-u5;



Factor * condition

Group NONE

SATISF ON				
QUALITY	0.391	0.081	4.855	0.000
CONTROL	-0.880	0.121	-7.247	0.000
QUALITY ON				
CONTROL	-0.871	0.128	-6.821	0.000
CONTROL ON				
UNDERST	-0.352	0.070	-5.022	0.000
UNDERST ON				
CGRAPH	0.530	0.132	4.025	0.000
Intercepts				
QUALITY	0.000	0.000	999.000	999.000
UNDERST	0.000	0.000	999.000	999.000



Factor * condition

Group NONE

SATISF ON				
QUALITY	0.391	0.081	4.855	0.000
CONTROL	-0.880	0.121	-7.247	0.000
QUALITY ON				
CONTROL	-1.001	0.146	-6.850	0.000
CONTROL ON				
UNDERST	-0.352	0.070	-5.022	0.000
UNDERST ON				
CGRAPH	0.530	0.132	4.025	0.000
Intercepts				
QUALITY	0.017	0.169	0.098	0.922
UNDERST	0.347	0.160	2.174	0.030



Factor * condition

Group NONE

SATISF ON				
QUALITY	0.391	0.081	4.855	0.000
CONTROL	-0.880	0.121	-7.247	0.000
QUALITY ON				
CONTROL	-0.359	0.117	-3.056	0.002
CONTROL ON				
UNDERST	-0.352	0.070	-5.022	0.000
UNDERST ON				
CGRAPH	0.530	0.132	4.025	0.000
Intercepts				
QUALITY	0.368	0.170	2.166	0.030
UNDERST	0.475	0.158	3.004	0.003

**“It is the mark of a truly intelligent person
to be moved by statistics.”**



George Bernard Shaw